

Sensor response of superhydrophobic quartz crystal resonators

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Overview

1. Superhydrophobic Surfaces

- Surface tension
- Topography and wetting
- Example surfaces

2. Fundamentals of Quartz Crystal Microbalances

- Gas and liquid phase QCM/QCR responses
- Hydrodynamics and boundary conditions
- Acoustic reflections and cavities

3. Superhydrophobic Surfaces on QCMs

- Theoretical concepts
- Types of surfaces
- QCM responses

Superhydrophobic Surfaces

The Natural World

Surface Tension

Surface Tension v Gravity

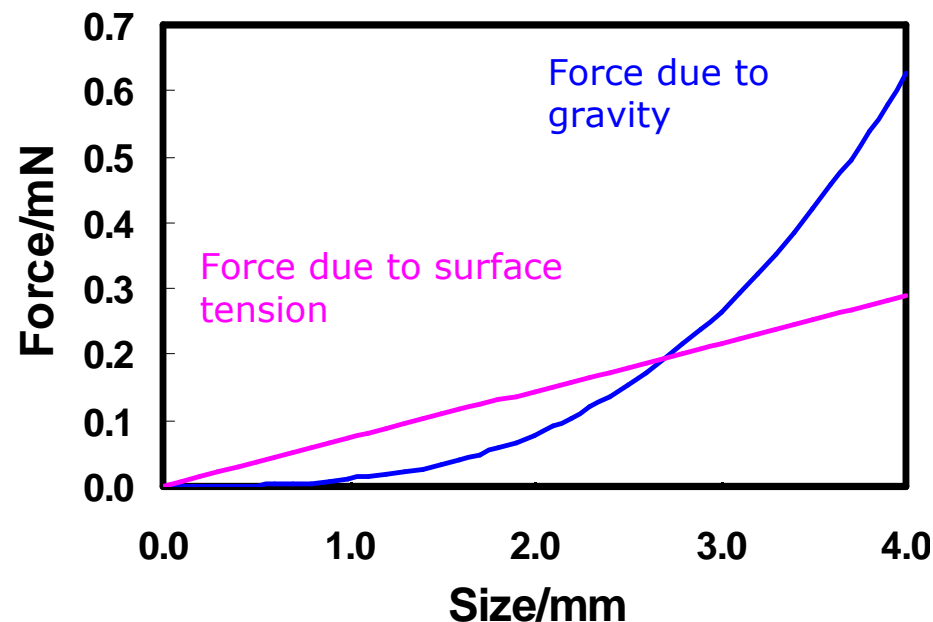
Surface tension forces scale with length, e.g. $\text{Force} \sim R\gamma_{LV}$

Gravity forces scale with length cubed, e.g. $\text{Force} \sim R^3\rho g$

Small sizes \Rightarrow surface tension wins

Small means \ll capillary length = $\kappa^{-1} = (\gamma_{LV}/\rho g)^{1/2} \sim 2.73\text{mm}$ for water

Winners v Losers



Acknowledgement Video: "Microcosmos"

The Sacred Lotus Leaf

Plants

Many leaves are super-water repellent

(i.e. droplets completely ball up and roll off a surface)

The Lotus plant is known for its purity

Superhydrophobic leaves are self-cleaning

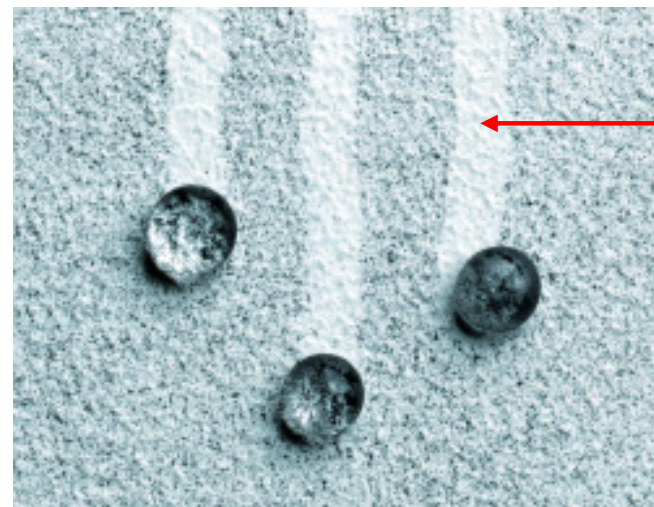
(under the action of rain)



SEM of a Lotus Leaf



Self-Cleaning



Dust
cleaned
away

Acknowledgement

Neinhuis and Barthlott

Plants and Leaves



Honeysuckle, Fat Hen, Tulip, Daffodil, Sew thistle (Milkweed), Aquilegia
Nasturtium, Lady's Mantle, Cabbage/Sprout/Broccoli

Superhydrophobic Surfaces

Man-made Surfaces

Water Repellency (Hydrophobicity)

Surface Chemistry

Terminal group determines whether surface is water hating

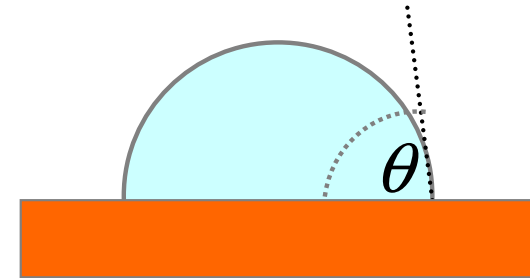
Hydrophobic terminal groups are Fluorine (F) and Methyl (CH_3)

Contact Angles

Characterize hydrophobicity

Water-on-Teflon gives $\sim 115^\circ$

The best that *chemistry* can do



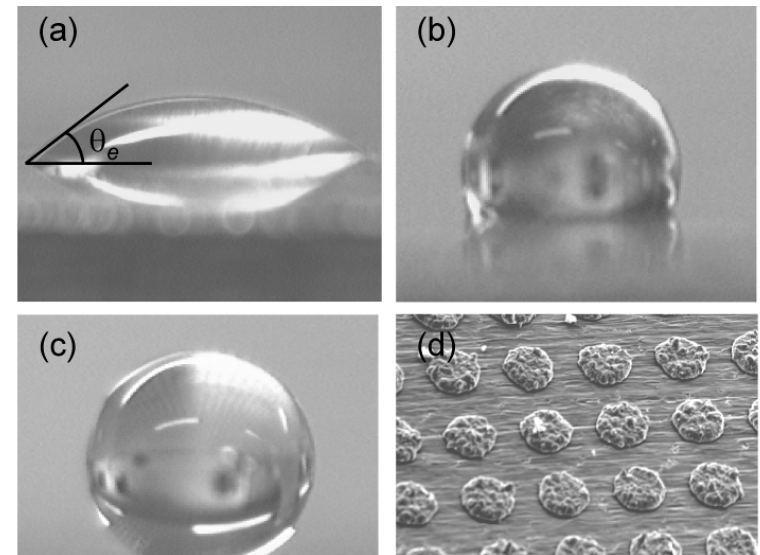
Physical Enhancement

(a) is water-on-copper

(b) is water-on-fluorine coated Cu

(c) is a super-hydrophobic surface

(d) "chocolate-chip-cookie" surface

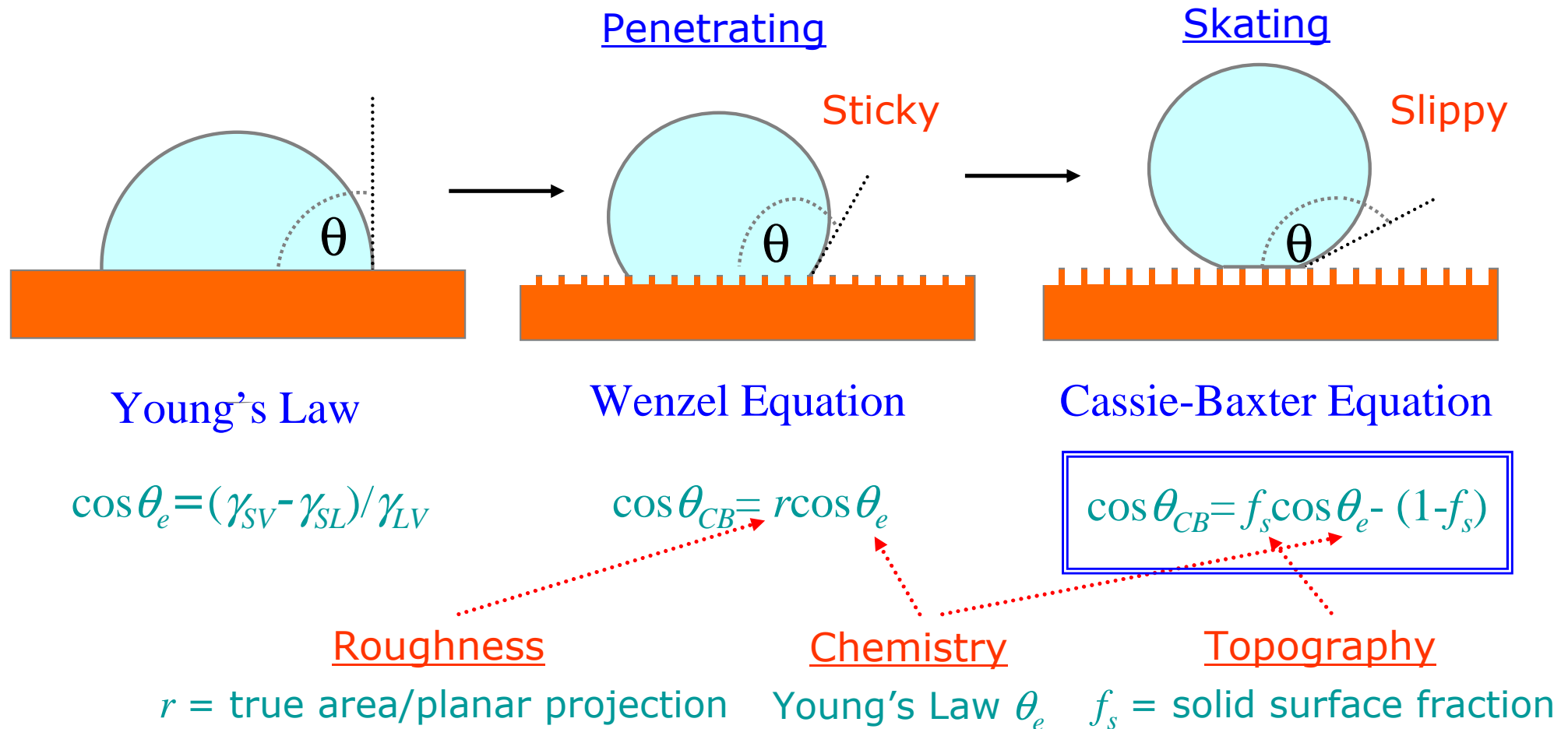


Superhydrophobicity is when $\theta > 150^\circ$
and contact angle hysteresis is low

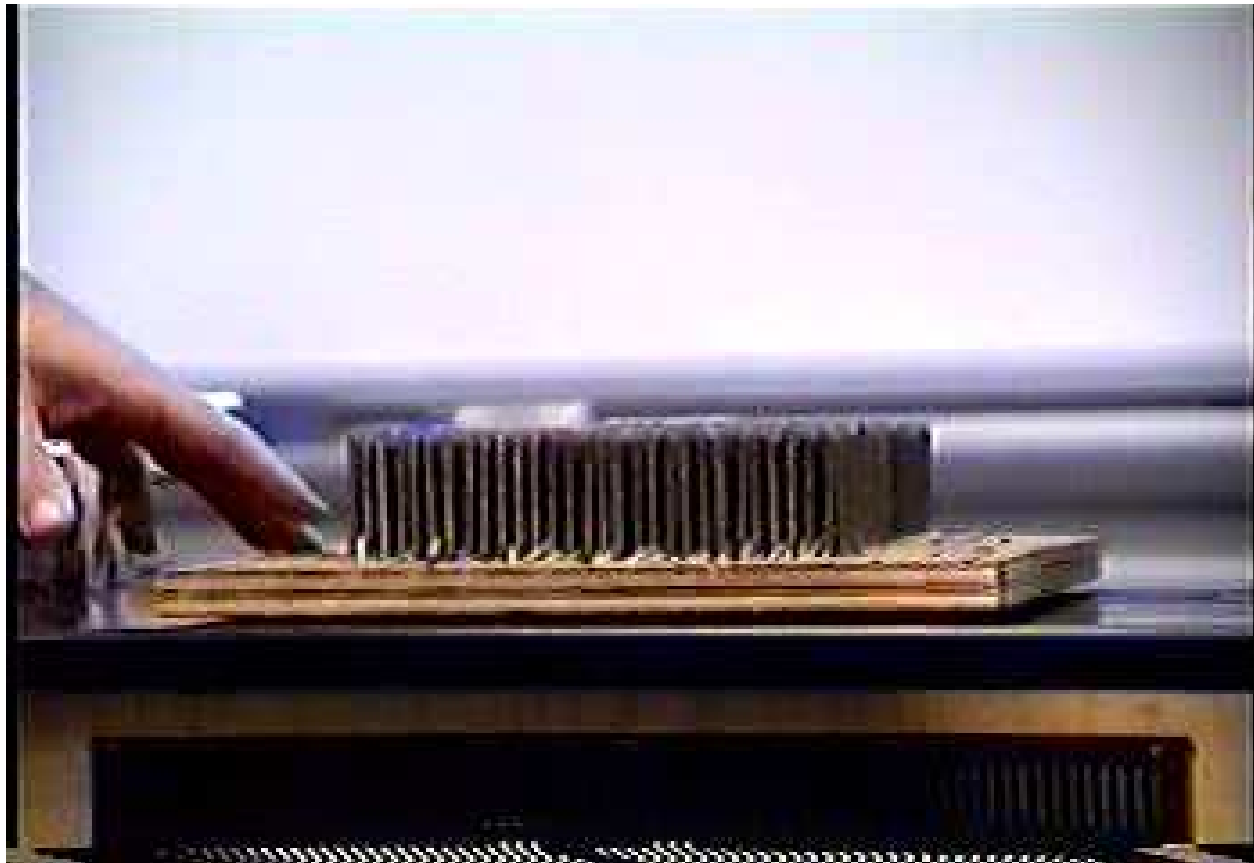
Topography & Wetting

Droplets that Skate

What contact angle does a droplet adopt on a “rough” surface?



Fakir's Carpet - "Bed of Nails" Effect



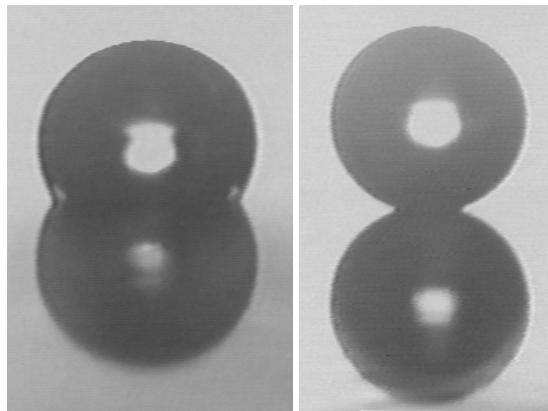
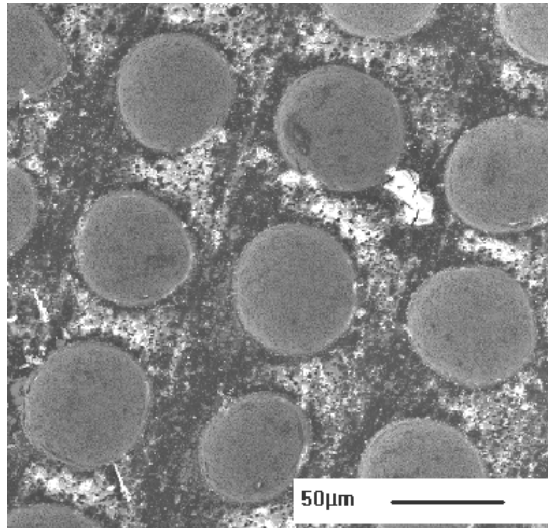
Balloon on a Bed of Nails

But liquid skin interacts with solid surfaces and "nails" do not need to be equally separated. A useful analogy, but it is not an exact view.

Acknowledgement Wake Forest University

Superhydrophobicity - Man-Made Examples

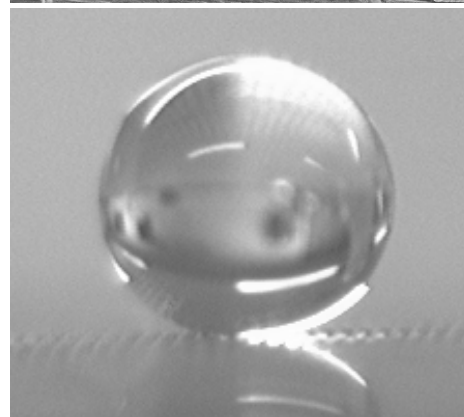
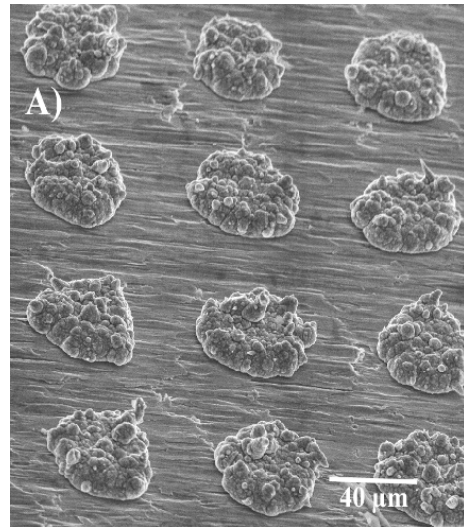
Etched Metal



Flat &
hydrophobic

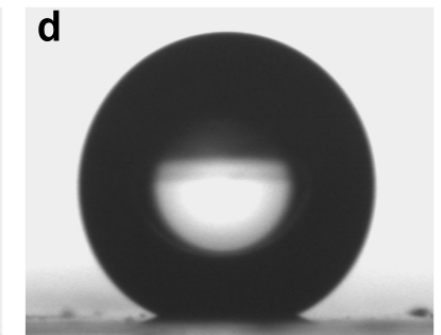
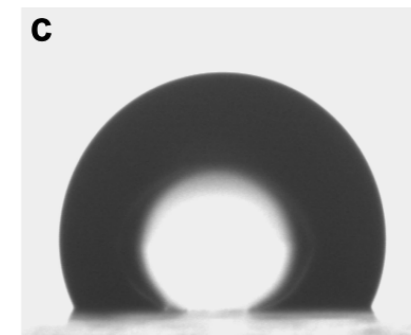
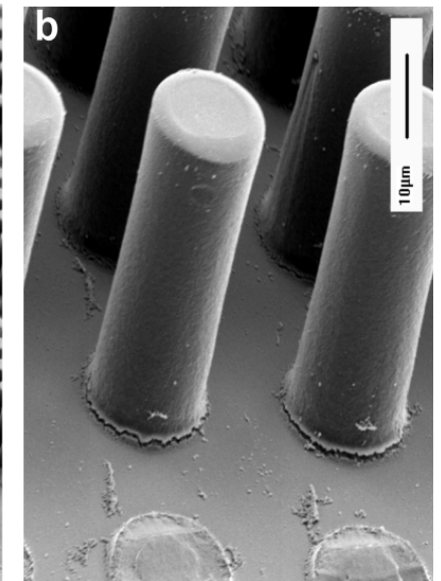
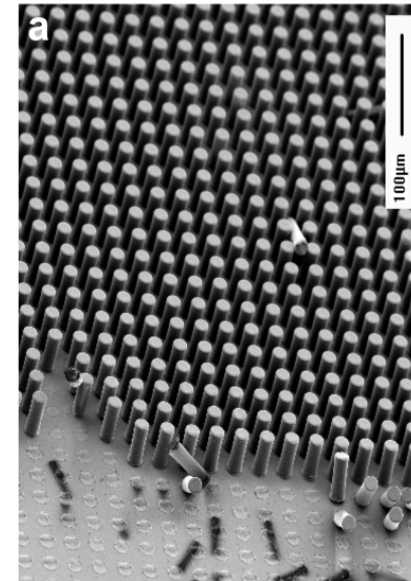
Patterned &
hydrophobic

Deposited Metal



Patterned &
hydrophobic

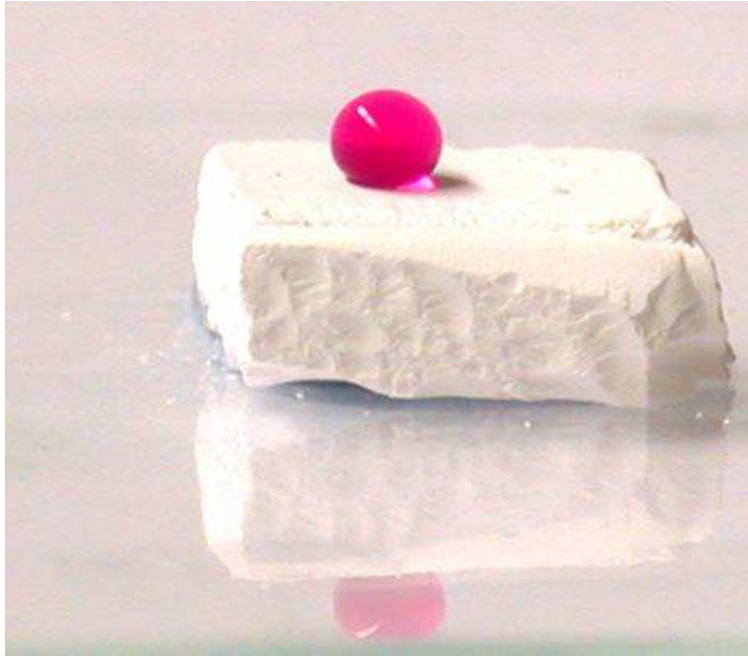
Polymer Microposts



Flat &
hydrophobic

Patterned &
hydrophobic

Sol-Gel: Switching off Superhydrophobicity



→
Foam heated
(and cooled)
prior to droplet
deposition

Mechanisms for Switching

- Temperature history of substrate
- Surface tension changes in liquid (alcohol content, surfactant, ...)
- Electrowetting

Switch could trigger a large change in QCM signal \Rightarrow Sensor based on hydrophobicity

Fundamentals of QCMs

Sensing Principles

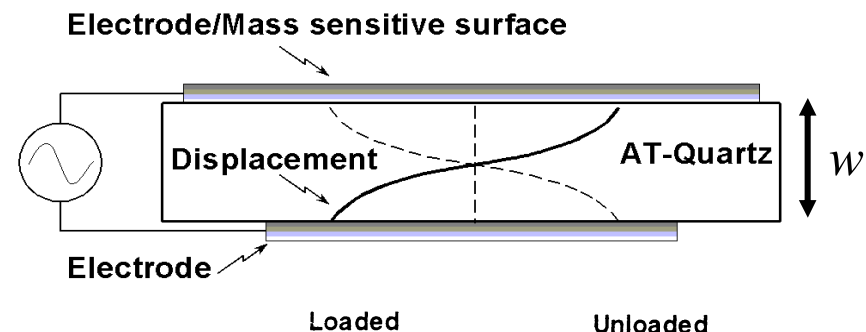
QCM/QCR Sensing Principles

Thickness Shear Mode Vibration

QCM has a sharp resonance

Frequency given by quartz thickness, w

$$v_s = f\lambda \Rightarrow f = 2v_s/w$$



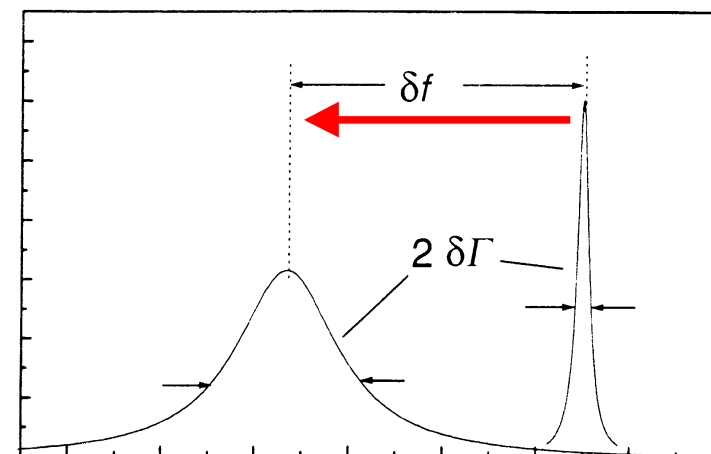
Mass Loading or Immersion

QCR resonant frequency reduces due to mass

Resonance broadens due to polymer/liquid

Sauerbrey equation $\Rightarrow \Delta f \propto -f^2 \Delta m/A$

Kanazawa & Gordon $\Rightarrow \Delta f \propto -\sqrt{(\eta\rho)} f^{3/2}$



1. Increasing mass or viscosity-density product decreases resonant frequency
2. Increasing viscosity-density product (or polymer) broadens resonance

Liquids and Penetration Depth

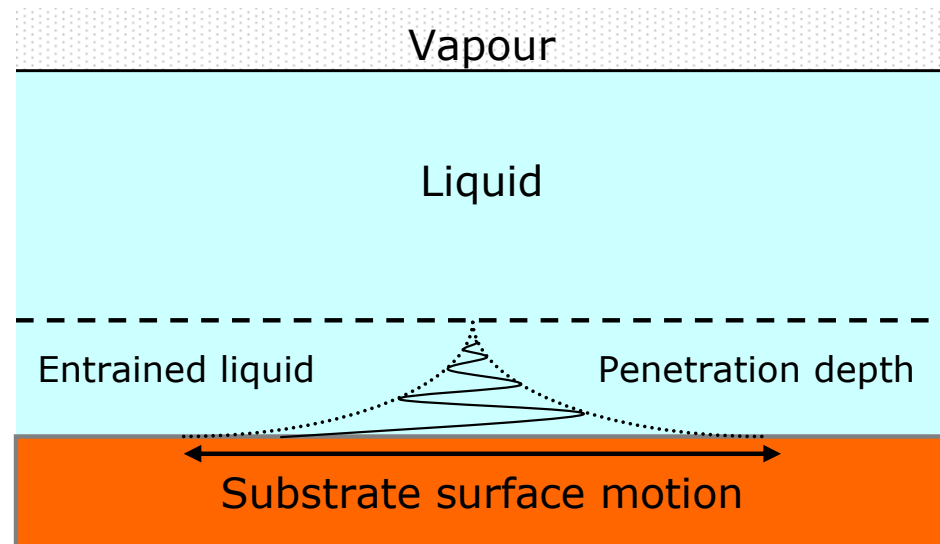
Shear Mode Vibration

Entraines liquid

Liquid oscillation decays

Penetration depth

$$\delta = (\eta / \pi f \rho)^{1/2}$$



Liquid Sensing

Sense liquid mass (via viscosity-density product) within penetration depth

QCM

SAW

For water:

5 MHz

$\delta \sim 250$ nm

500 MHz

$\delta \sim 25$ nm

1. Penetration depth gives sensing zone which decreases with frequency
2. Penetration depth/sensing zone increases with viscosity

Hydrodynamic View

Mathematical Formulation

Wave equation for substrate and solid layer or Navier-Stokes equations for liquid
define substrate and layer/fluid displacements

Match solutions at boundary (substrate-air, substrate-layer or substrate-liquid)

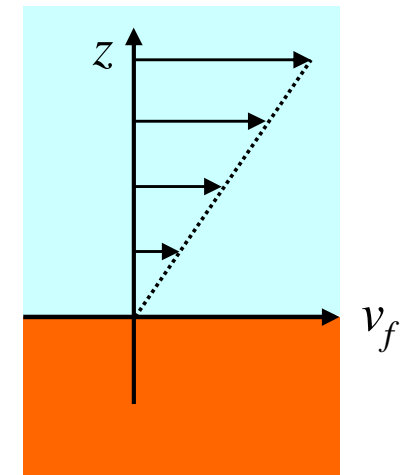
Provides dispersion equation and solution gives resonances

No-Slip Boundary Condition

Solid-Air $\Rightarrow q_s(z=0)=q_l(z=0)$ substrate & layer displacements
match at all times

i.e. $v_s(z=0)=v_l(z=0)$ speeds at wall match

Solid-Water $\Rightarrow v_s(z=0)=v_f(z=0)$ speeds at wall match - fluid
speed extrapolated from bulk

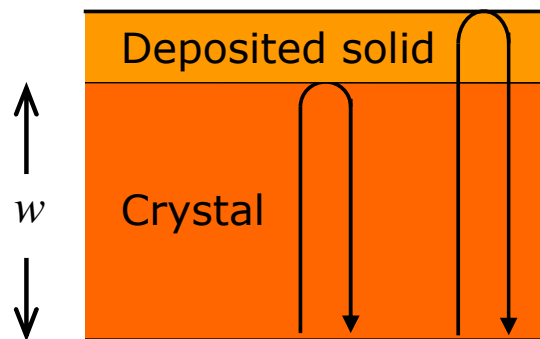


Acoustic Reflection View

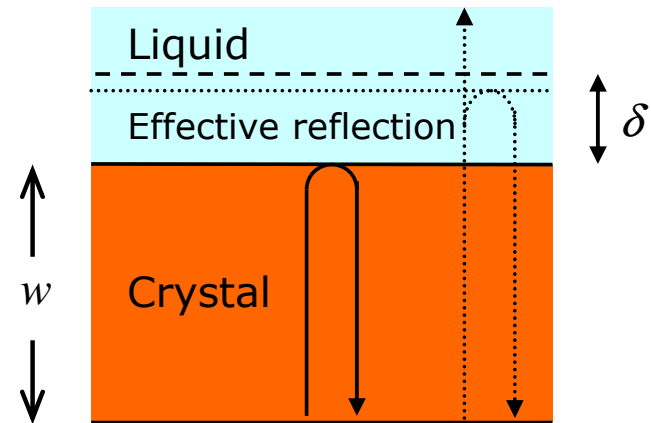
Simple Cavities and Standing Waves

Solid-Air \Rightarrow Uniform and strong reflection

Solid-Water \Rightarrow Partial reflection at an effective plane within penetration depth



Cavity length increases: f_{\downarrow}
Reflection remains strong



Cavity length increases: f_{\downarrow}
Reflection becomes partial: B_{\uparrow}

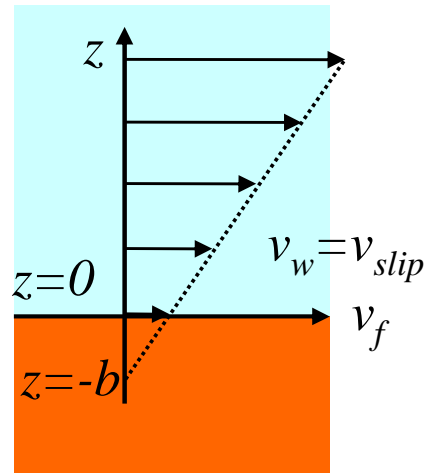
Superhydrophobic QCMs

Theoretical Concepts

Mathematical Formulation of Wall Slip

Flow Profile

With slip length, b



Slip length, b , models effective position of interface
 Negative b implies effective interface moves to
 liquid side of boundary

Equations

Match speeds

$$v_s(z=0) = v_f(z=-b)$$

Expand

$$v_w - v_f(z=0) = -b \left(\frac{\partial v_f}{\partial z} \right)_{z=0}$$

Force exerted on wall
 divided by viscosity

*Slip length is a mechanism for modelling an effective average boundary
 and/or taking into account liquid-solid interfacial forces*

Effective Sauerbrey “Liquid Mass”

Equations of Motion

Solve with slip boundary condition for acoustic impedance
Consider in terms of slip length and
interpret solution for small b

$$Z_L^{slip} \approx \frac{Z_L^{no\ slip}}{1 + \frac{b}{\eta_f} Z_L^{no\ slip}}$$

Newtonian Liquid

Kanazawa & Gordon result for no-slip
modified by “slip” correction using b/δ

$$\left(\frac{\Delta\omega}{\omega}\right)_{slip} \approx \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} \left(1 - \frac{2b}{\delta}\right)$$

Slip length to penetration depth ratio

Negative Slip Length

Define a liquid mass as $\Delta m_f = b\rho_f$

$$\left(\frac{\Delta\omega}{\omega}\right)_{additional} \approx \left(-\frac{2b}{\delta}\right) \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} = \frac{\omega\Delta m_f}{\pi\sqrt{\mu_s\rho_s}}$$

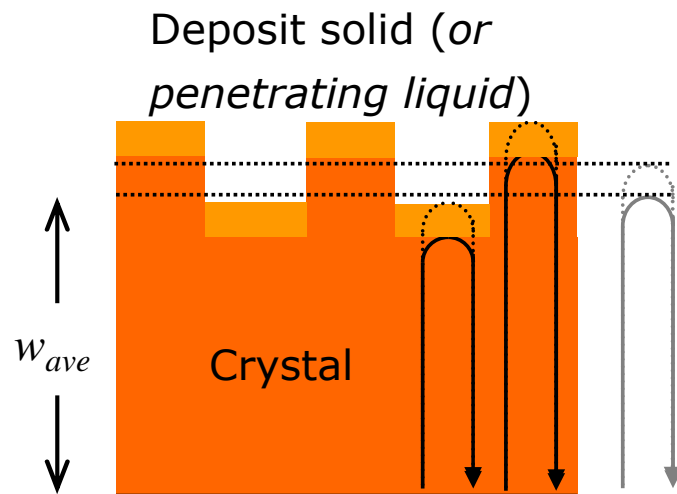
Trapped “Sauerbrey liquid mass” + Kanazawa & Gordon viscosity-density product contribution, but assumes all locations are equal, i.e. complete liquid penetration.

Acoustic Reflection View

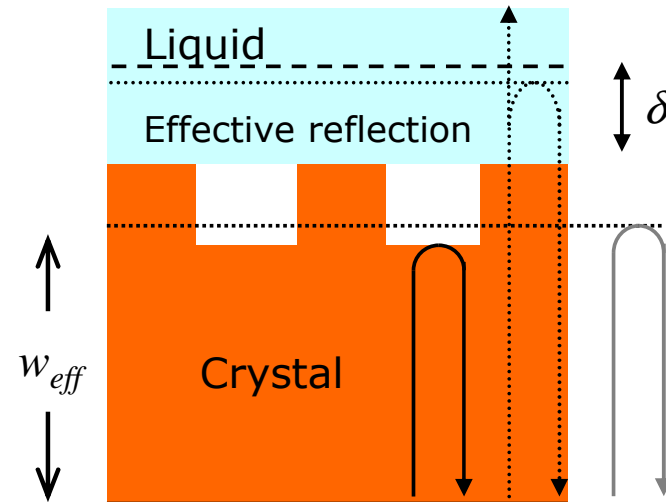
Structured Cavities and Standing Waves

Air contact \Rightarrow Equally strong reflections from peaks and troughs of surface

Water contact \Rightarrow Changes cavity length and strength of reflection defined by peaks



Effective cavity length
Peaks and trough increase
cavity lengths equally: f_{\downarrow}

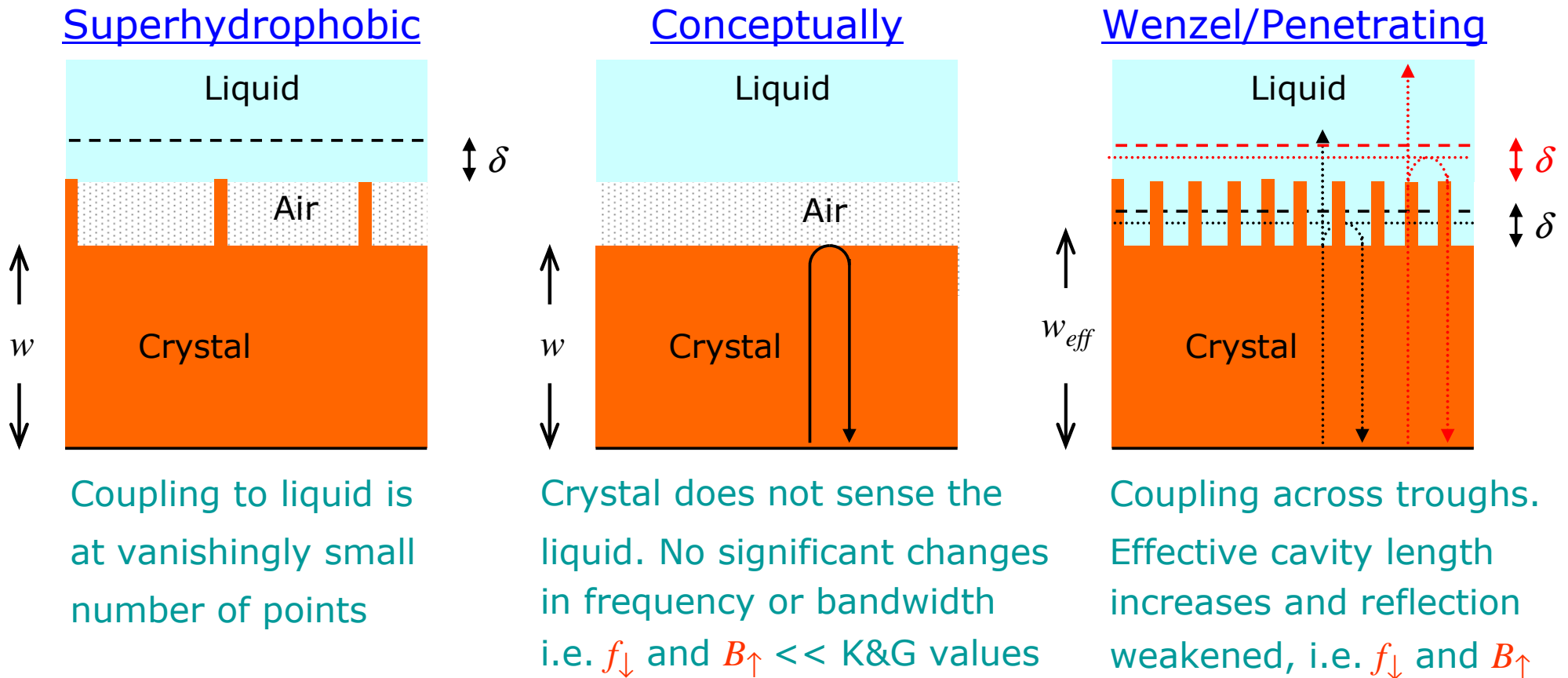


Effective cavity length increased? i.e. f_{\downarrow}
Or top reflection weakened? If so,
effective cavity length decreased: f_{\uparrow}

Skating form of superhydrophobicity offers possibility of new liquid phase responses

Extreme Superhydrophobic Case

Water immersion \Rightarrow Water skates across surface features and pressure (or other force) is needed to force capillary penetration



QCM behaves as if decoupled from the liquid, unless liquid penetrates into structure

Experiments with QCMs

Superhydrophobic Surfaces

Superhydrophobic Surfaces on QCM's

Previous Literature Data on QCMs

1. Polyethylene glycol-water on a hydrophobic SU-8 micro-post QCM¹,
Polystyrene with embedded PTFE based superhydrophobic surface², 0.6 μm
silica nanoparticle layer superhydrophobic multiresonance device³
2. Water-glycerol on hydrophobic model system of SU-8 micro-posts (5 μm
diameter, 10 μm centre-centre, 5-18 μm tall) QCM's⁴

Experimental Data in this Talk

1. Review SU-8 micro-post data (5 μm , 138°; 10 μm , 143°; 15 μm , 151°; 18 μm , 155°)
2. New data using water-glycerol mixtures (0-80%), contact angles, BVD
impedance fitting, bare (non-hydrophobised) & hydrophobised (Granger's)
3. Surfaces based on nano-particles

Titanium dioxide sol-gel (porous 1 μm) + Granger's

Before QCM experiment: 154°

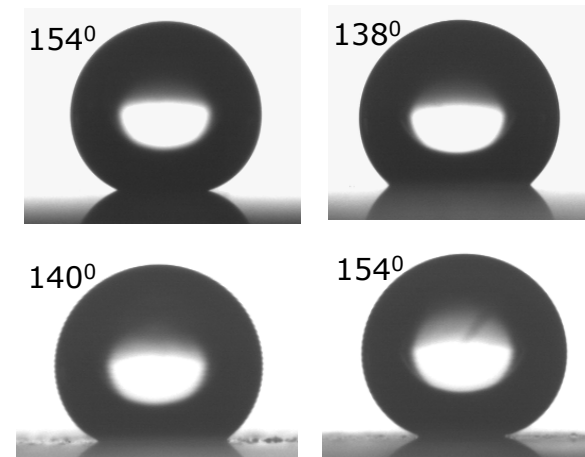
After QCM experiment: 138° (immobile)

Organo-silane treated silicon dioxide particles
dusted onto 1.7 μm S1813 photoresist

Two samples of different particle sizes:

a1=5 nm. After experiment: 140° (immobile)

b1=3 nm. After experiment: >154° (mobile)



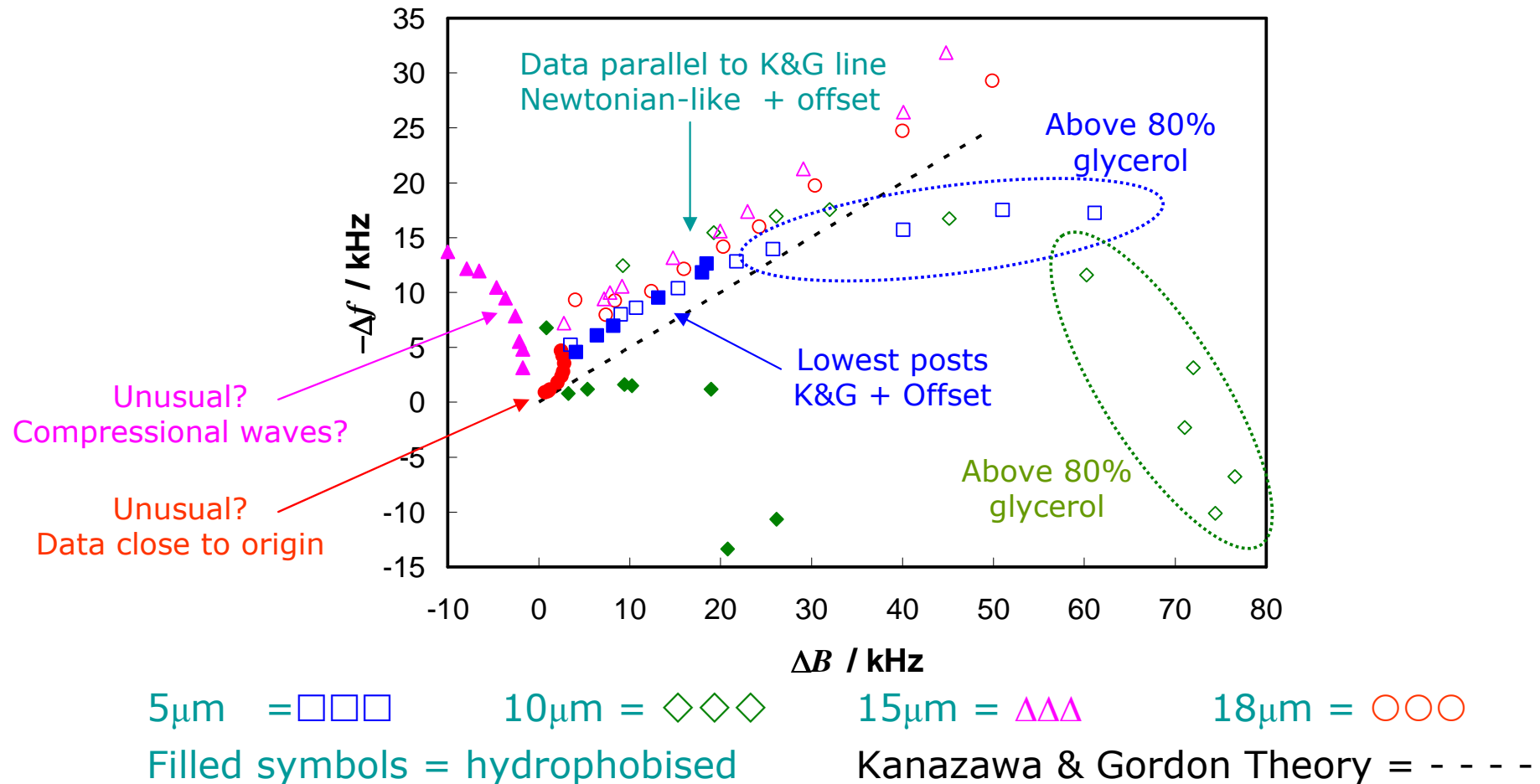
References ¹Evans, C., *et al.*, Sens. Act. A 123-24 (2005) 73-76; ²Fujita, M., *et al.*,
Jan. J. Appl. Phys., 44 (2005) 6726-6730; ³Kwoun, S.J., *et al.*, IEEE Trans. Ultrason.
Ferroel. Freq. Ctrl 53 (2006) 1400-1403. ⁴Roach, P., *et al.* Langmuir 23 (2007) 9823-9830.

Experiments with QCMs

Superhydrophobic Micro-post Data

Micro-Post Surfaces – Newtonian or Not?

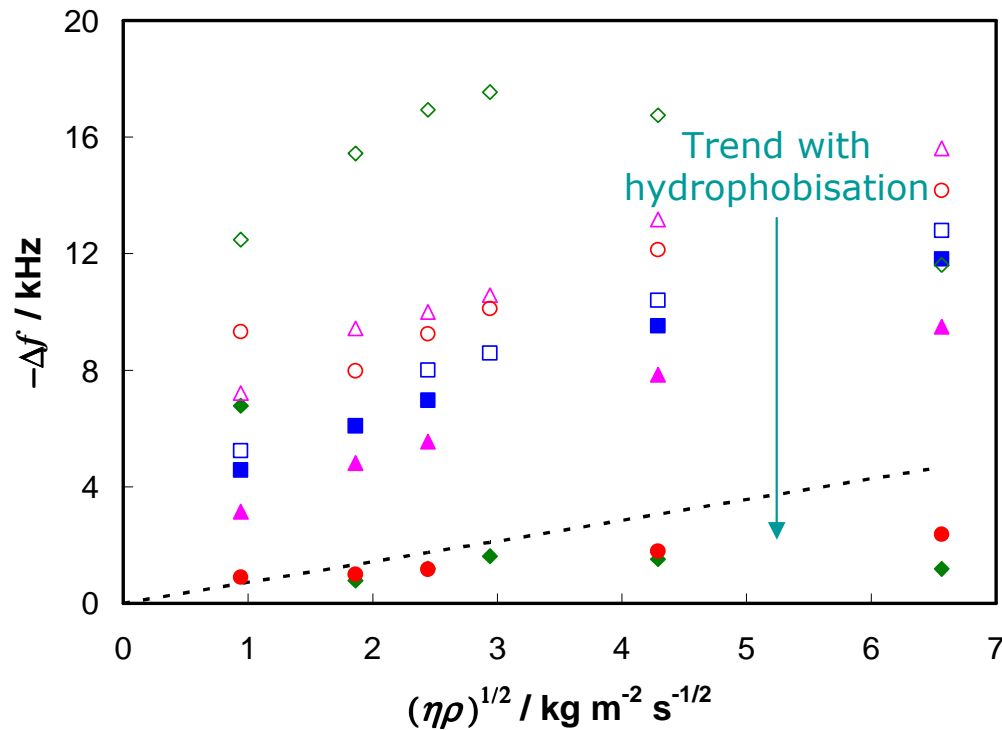
Bare (non-hydrophobised) and Hydrophobised (0-100%)



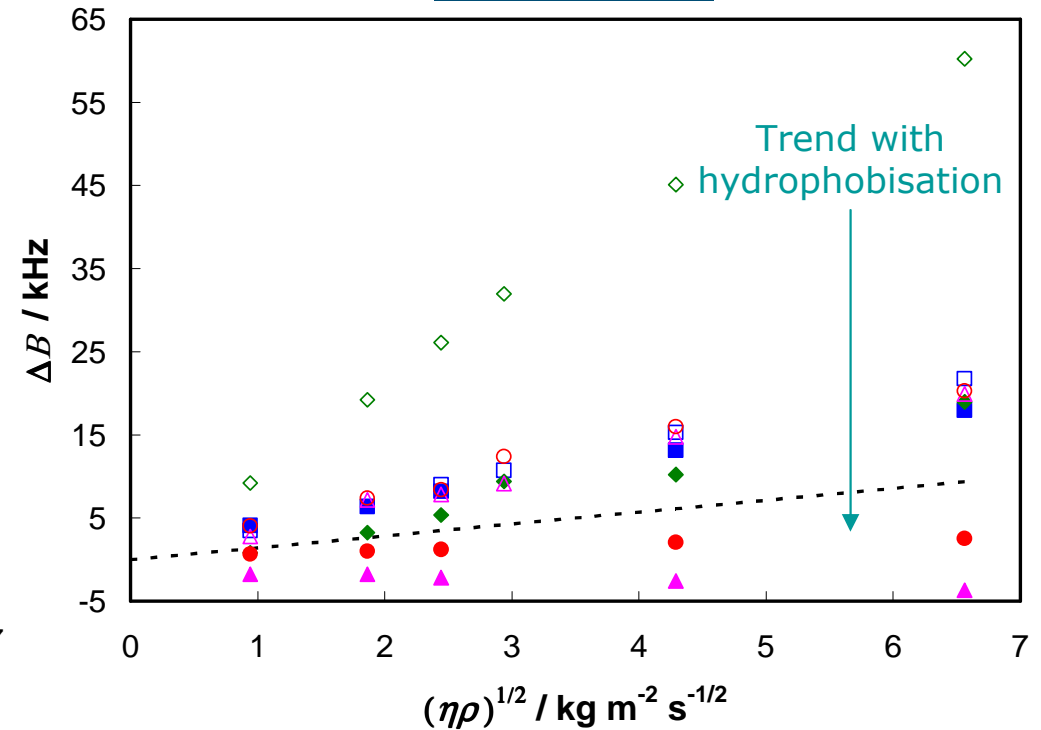
Hydrophobisation of posts changes type of response – all data generally closer to origin

Micro-Post Surfaces: Viscosity-Density

Frequency



Bandwidth



5μm = □□□

10μm = ◇◇◇

15μm = △△△

18μm = ○○○

Filled symbols = hydrophobised

Kanazawa & Gordon Theory = - - - -

Tallest (18 μm) hydrophobic posts have coupling to liquid reduced below K&G levels

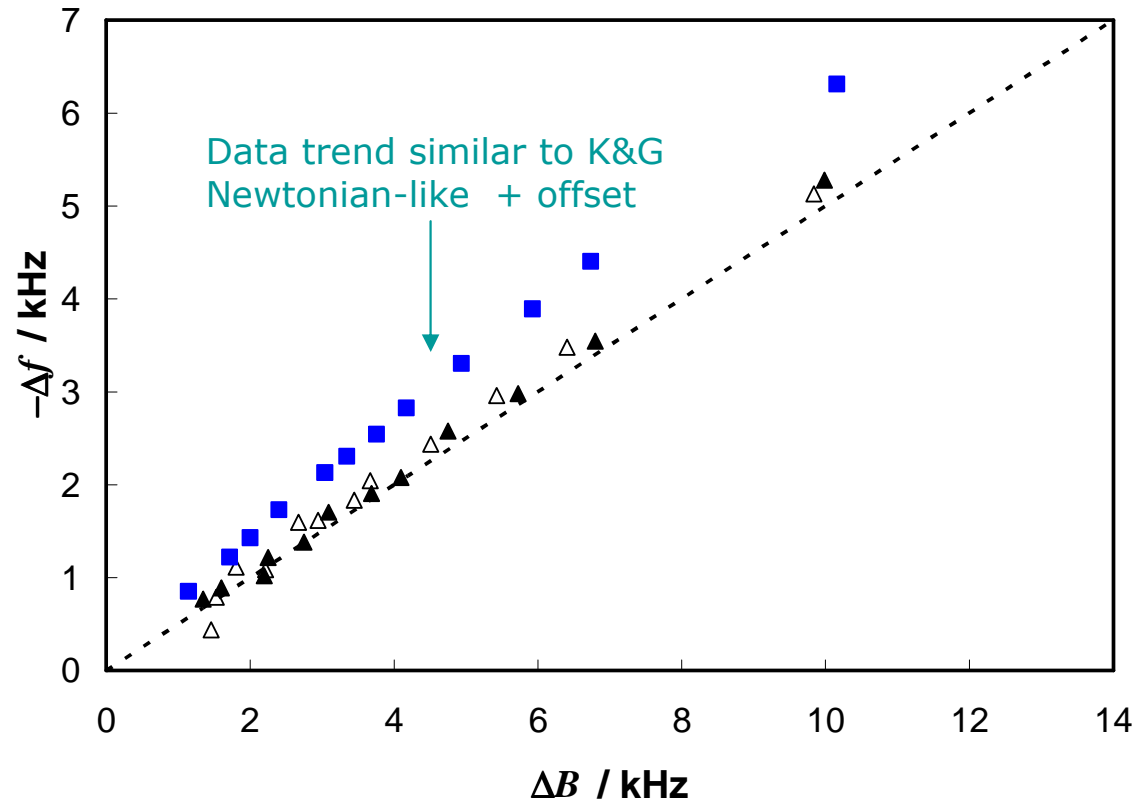
15 μm tall posts have unusual dB response (compressional wave generation?)

Experiments with QCMs

Hydrophobic Titanium Dioxide Data

Hydrophobic TiO_2 Surfaces – Newtonian or Not?

Water-glycerol solutions: 0-80%



Blank at 25 °C = $\triangle\triangle\triangle$

Hydrophobic crystal at 20 °C = $\blacktriangle\blacktriangle\blacktriangle$

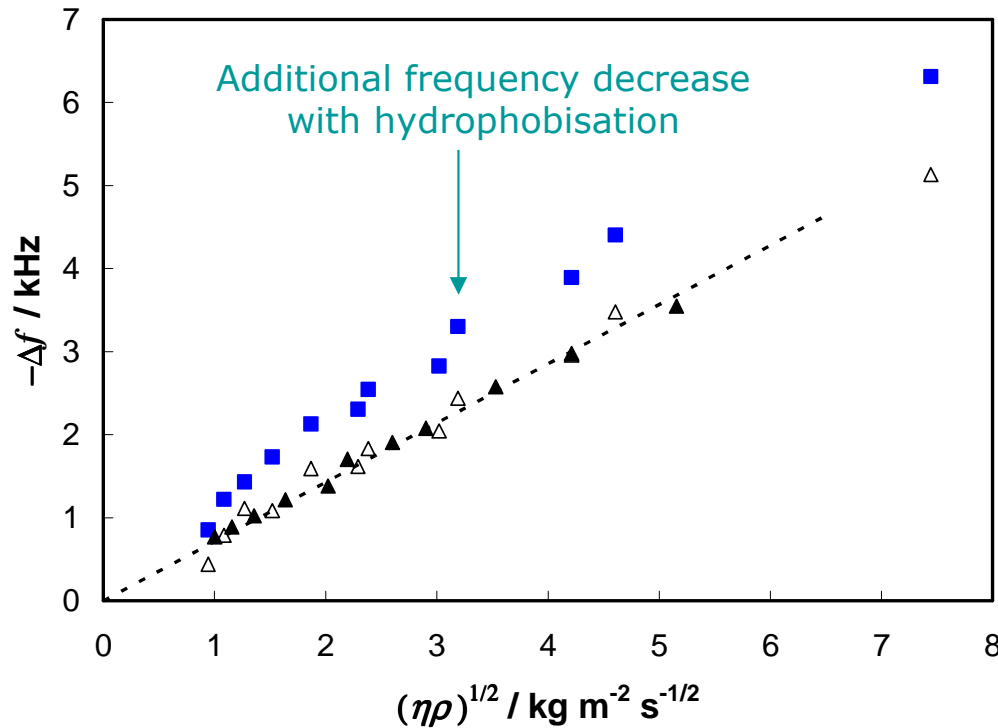
Hydrophobic TiO_2 = $\blacksquare\blacksquare\blacksquare$ at 25 °C

Kanazawa & Gordon Theory = - - - -

Newtonian-like + offset type of response

TiO₂ Surfaces: Viscosity-Density

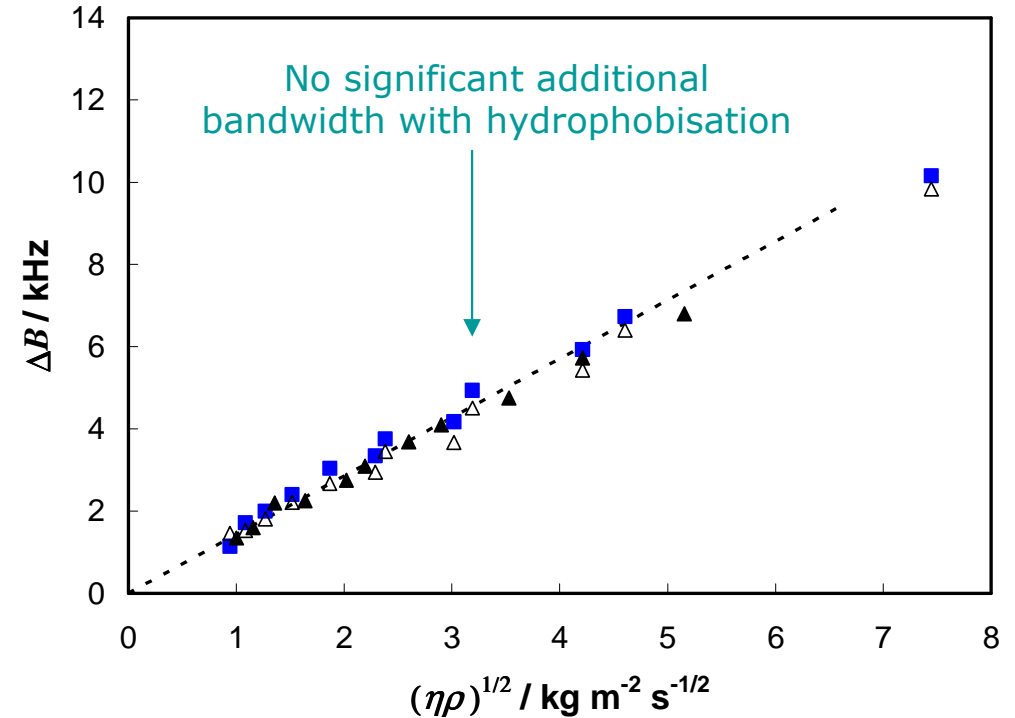
Frequency



Blank at 25 °C = $\triangle\triangle\triangle$

Hydrophobic crystal at 20 °C = $\blacktriangle\blacktriangle\blacktriangle$

Bandwidth



Hydrophobic TiO₂ = $\blacksquare\blacksquare\blacksquare$ at 25 °C

Kanazawa & Gordon Theory = - - - -

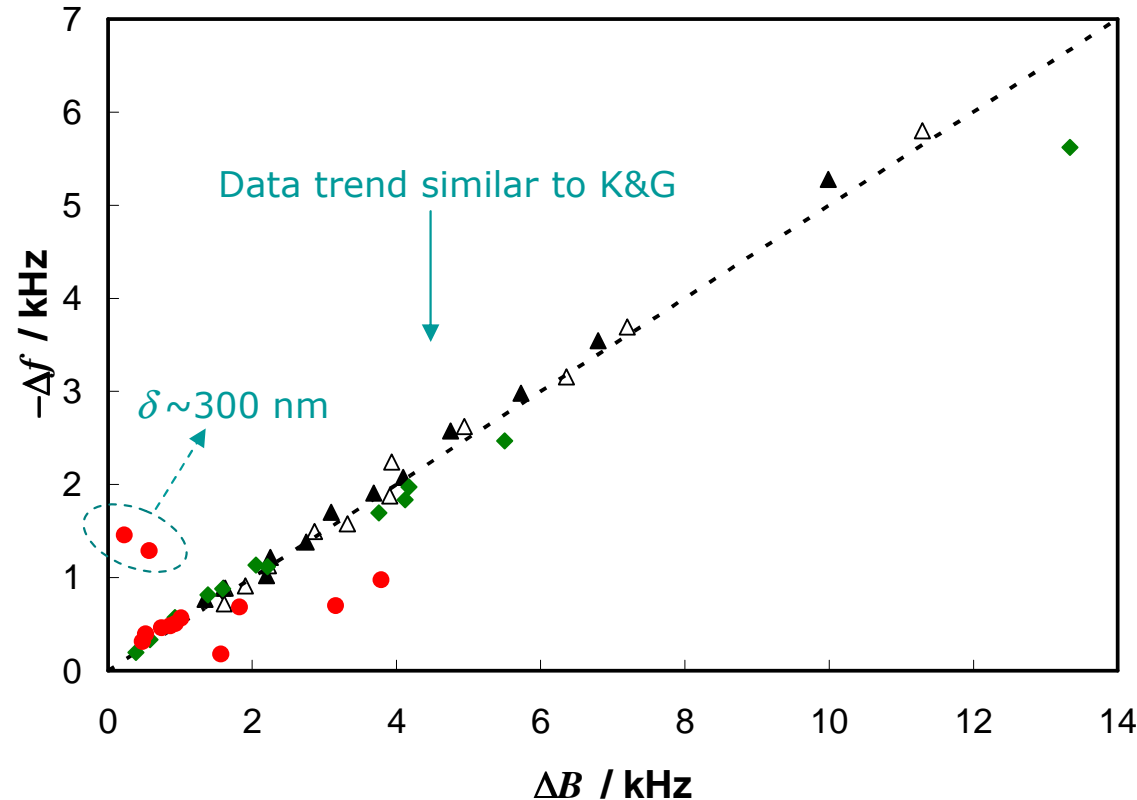
Shift is an additional frequency decrease beyond K & G rather than in dB. Consistent with "rigid liquid mass" from penetrating/Wenzel liquid (contact angle data/immobile drop)

Experiments with QCMs

Superhydrophobic Silicon Dioxide Data

Hydrophobic SiO₂ Surfaces – Newtonian or Not?

Water-glycerol solutions: 0-80%



Blank at 25 °C = $\Delta\Delta\Delta$

Hydrophobic crystal at 20 °C = $\blacktriangle\blacktriangle\blacktriangle$

ΔB / kHz

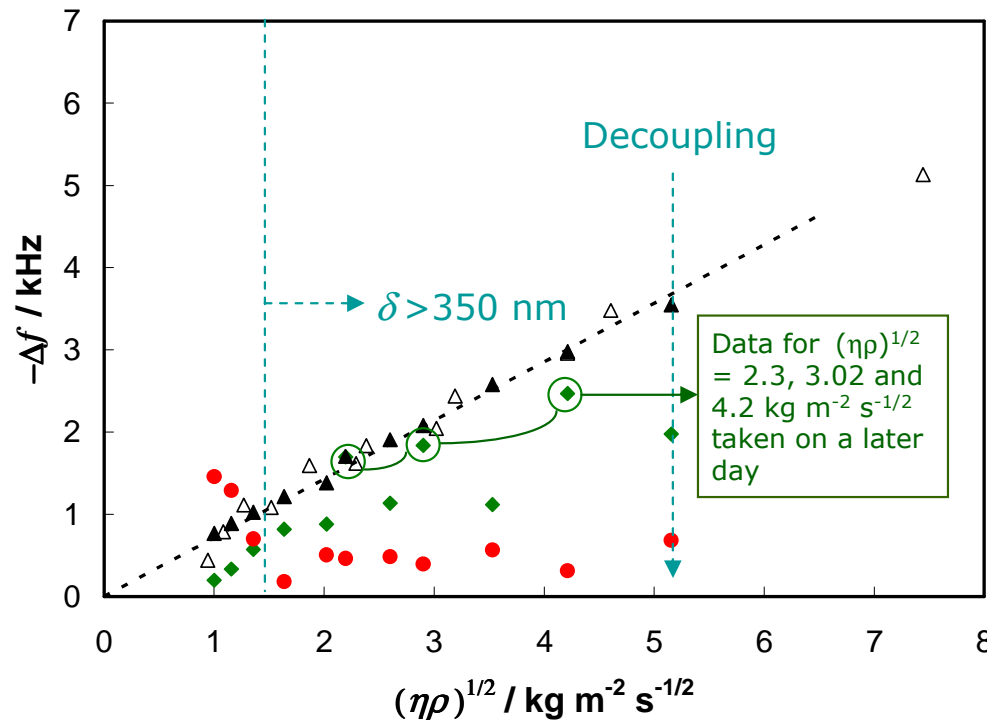
a1 (Super?)hydrophobic SiO₂ = $\blacklozenge\blacklozenge\blacklozenge$ at 20 °C

b1 Superhydrophobic SiO₂ = $\bullet\bullet\bullet$ at 20 °C

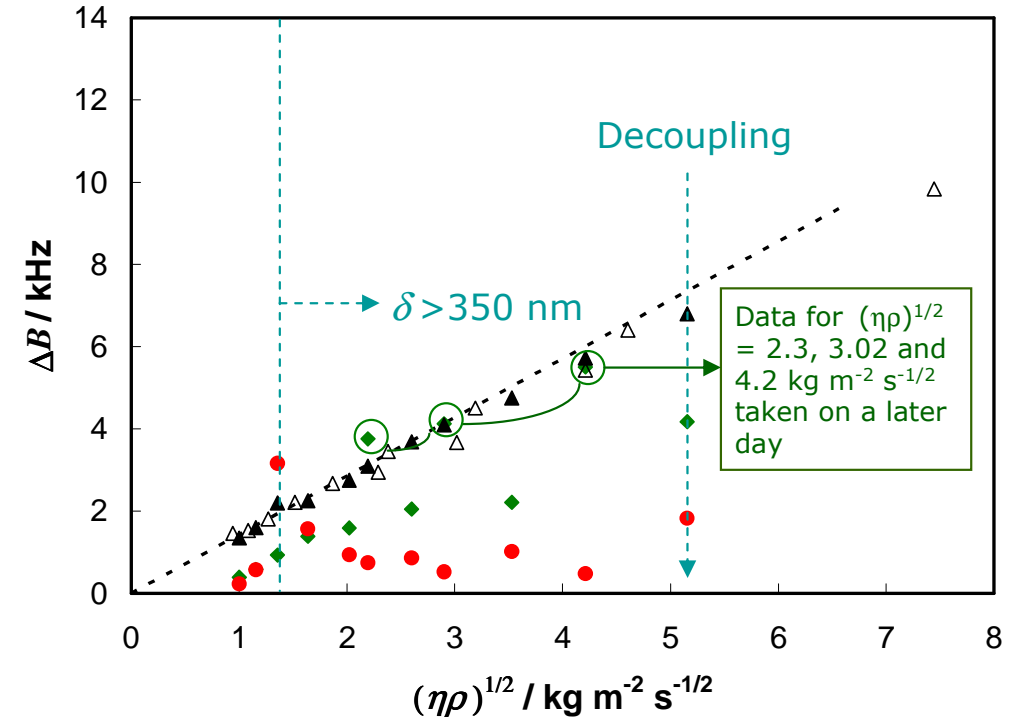
Data for a1 surface is Newtonian-like. Data for b1 is closer to origin, but more scattered

SiO₂ Surfaces: Viscosity-Density

Frequency



Bandwidth



Blank at 25 °C = ΔΔΔ

Hydrophobic crystal at 20°C = ▲▲▲

a1 (Super?)hydrophobic SiO₂ = ◆◆◆ at 20 °C

b1 Superhydrophobic SiO₂ = ●●● at 20 °C

a1: most data points show reduction below K&G levels, later data are at K&G levels

b1: data has stronger decoupling trend – consistent with contact angle data/mobile drop

Conclusions

1. Surface Chemistry Changes QCM Sensor Response

Type of effect on rough/structured surface depends on aspect ratio

Type of effect depends on whether gas-liquid-vapor interfaces exist

2. Penetrating/Wenzel Form of Wetting Occurs for

Hydrophobic 5 μm tall posts and hydrophobic TiO_2

Hydrophobic TiO_2 follows expected trends of “trapped liquid mass”

$|\Delta f|$ larger than predicted by Kanazawa & Gordon and $|\Delta B| \sim$ K&G prediction

Hydrophobic 5 μm tall posts roughly follows trends of “trapped liquid mass”

$|\Delta f|$ larger than predicted by Kanazawa & Gordon and $|\Delta B|$ “slightly” $>$ K&G prediction

3. Skating/Cassie-Baxter Form of Wetting Occurs for

Hydrophobic 18 μm tall posts and b1 superhydrophobic SiO_2

Both follow expected trends from acoustic reflection view

Both $|\Delta f|$ and $|\Delta B|$ much smaller than K&G prediction

4. Other Comments

a1 (super?)hydrophobic SiO_2 surface was unstable becoming a Wenzel surface

Penetration depth \sim surface feature size may create resonances

Acknowledgements

1. IEEE FCS Technical Programme Committee

Invitation to talk

2. Internal Collaborators

Dr Mike Newton (Concepts and QCM experimental development)

Dr Neil Shirtcliffe (Materials methods)

Dr Paul Roach (Materials methods and QCM experiments)

Dr Carl Evans, Mr Steve Elliott (QCM experiments)

3. External Colleagues who've motivated and discussed work

Dr Ralf Lücklum

Professor Mike Thompson, Dr Gordon Hayward, Mr Jon Ellis

4. Funding Agencies

EPSRC Grant EP/D500826/1

Dstl/Dr Stuart Brewer

The End

Key Parameters and Length Scales?

Superhydrophobicity

Gaps less than capillary length of liquid ~ 2.73 mm for water

Aspect ratio = height-to-lateral separation of features > 1

Cassie-Baxter contact angle $> 150^\circ$

Typically, solid surface fraction, $f_s < 20\%$ and hydrophobicity of surface, $\theta_e \sim 110^\circ$

Low contact angle hysteresis ($< 5^\circ$) so droplet rolls easily

Decoupling QCM

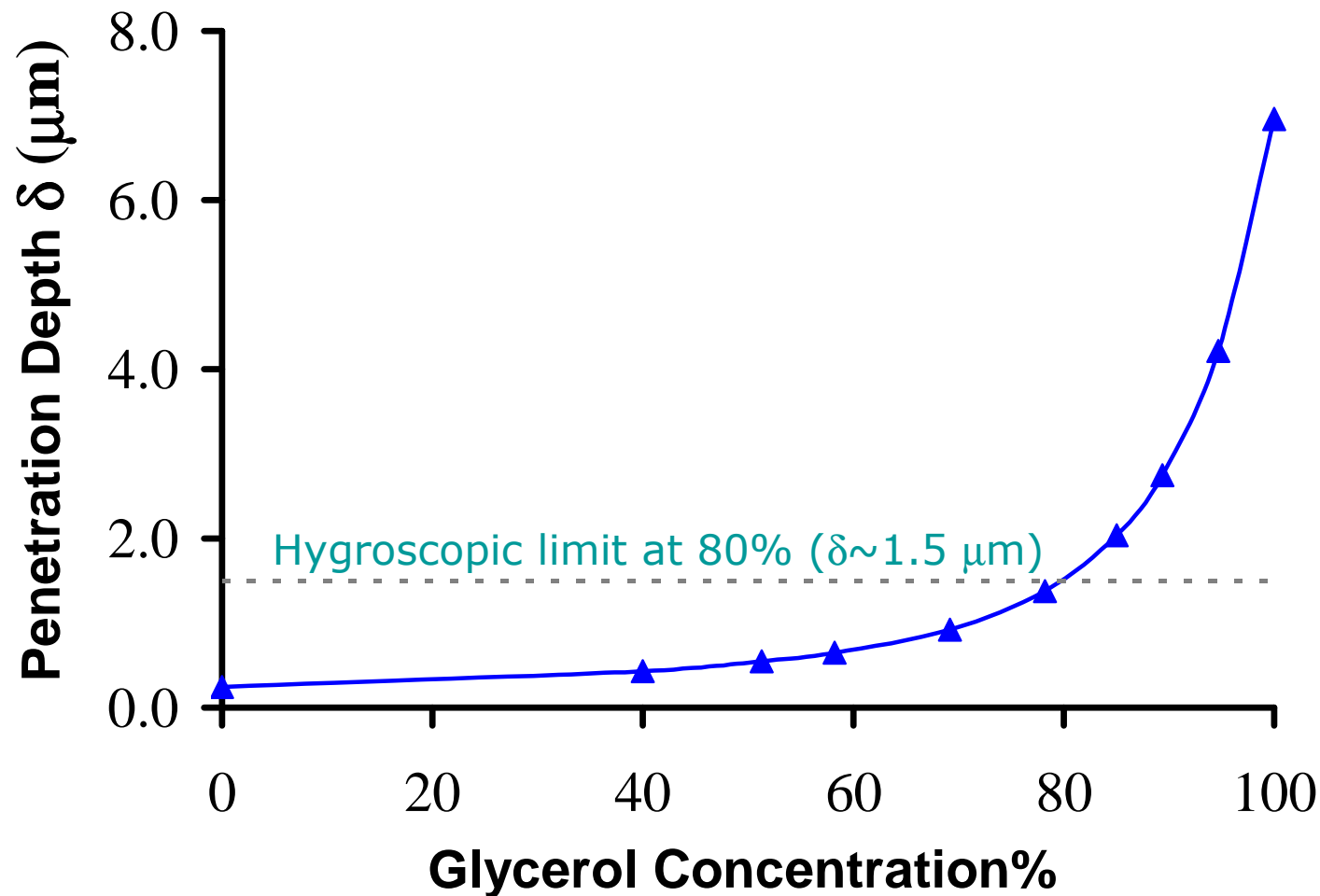
Low solid surface fraction (so reflection from troughs dominates)

Lateral separation of features $>$ penetration depth

Height of features compared to penetration depth?

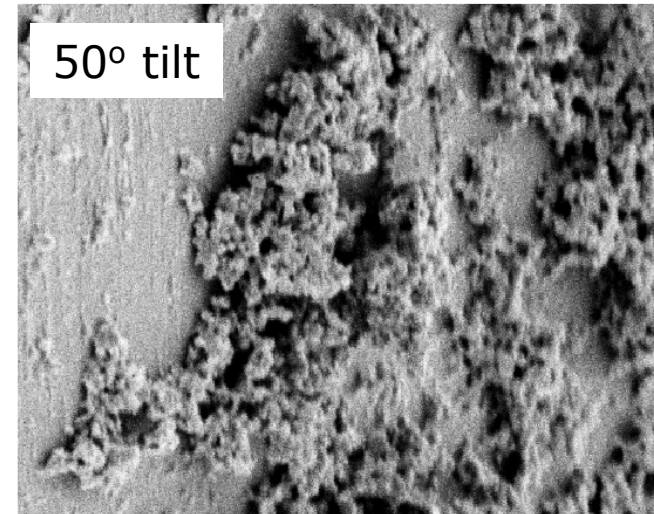
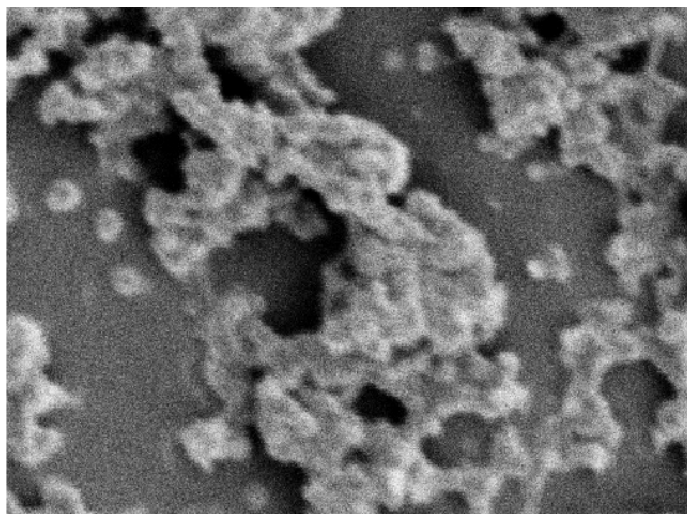
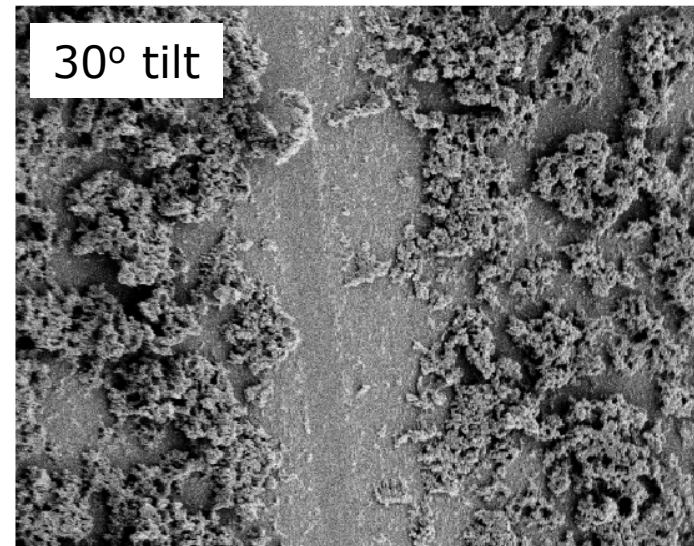
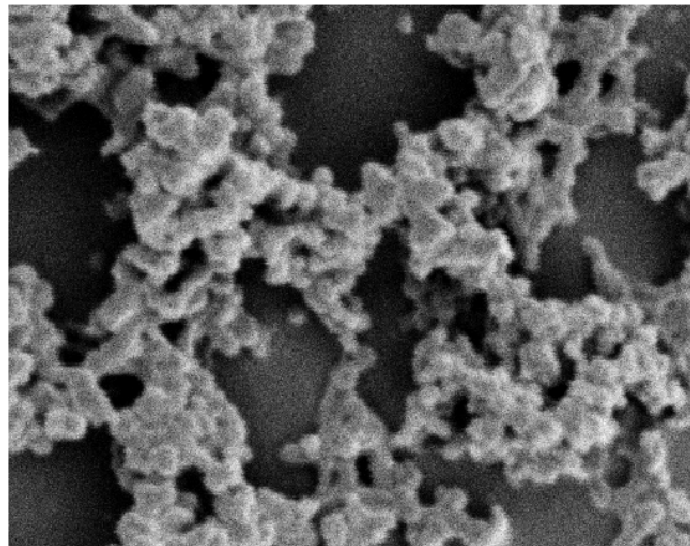
Acoustic reflection coefficient for substrate-liquid interface?

Water-Glycerol Mixtures - Penetration Depth

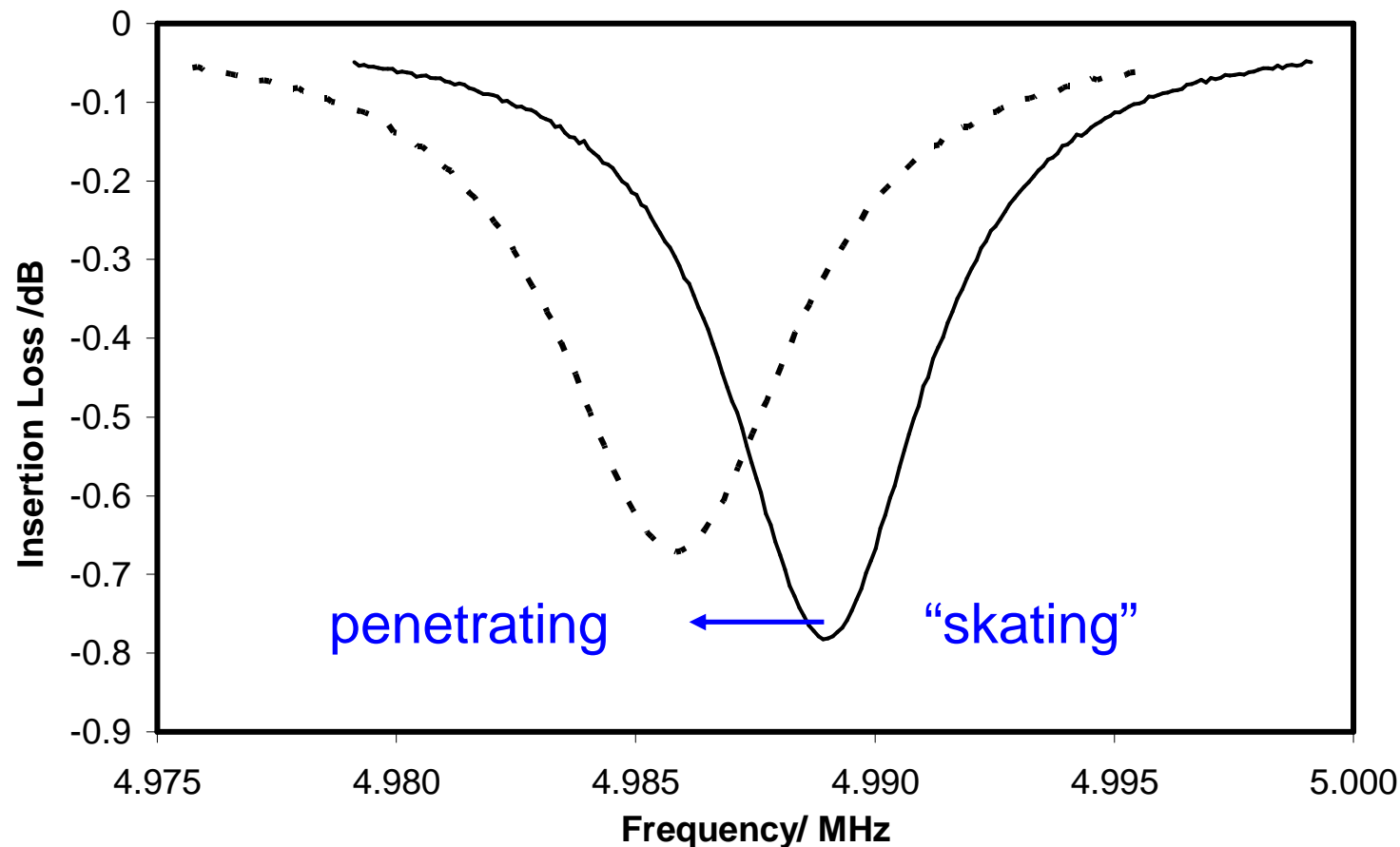


QCM behaves as if decoupled from the liquid, unless liquid penetrates into structure

TiO₂ sol-gel + Granger's coating



QCM Confirmation of “Skating”



Hydrophobised 18 μm micro-posts. Solid-line is Before pressure applied. Dotted curves is after pressure is applied.

Visually confirmed water ingress after pressure applied